

6.10 Writing Equations of Circles HW

Directions: Write the equation of the circle in STANDARD form.

1) $x^2 + 2x + y^2 - 10y + 10 = 0$

$$x^2 + 2x + \underline{1} + y^2 - 10y + \underline{25} = -10 + \underline{1} + \underline{25}$$

$$(x+1)^2 + (y-5)^2 = 16$$

2) $x^2 + y^2 - 4x + 6y + 9 = 0$

$$x^2 - 4x + y^2 + 6y = -9$$

$$x^2 - 4x + \underline{4} + y^2 + 6y + \underline{9} = -9 + \underline{4} + \underline{9}$$

$$(x-2)^2 + (y+3)^2 = 4$$

3) $x^2 + y^2 - 10x - 12y + 40 = 0$

$$x^2 - 10x + \underline{25} + y^2 - 12y + \underline{36} = -40 + \underline{25} + \underline{36}$$

$$(x-5)^2 + (y-6)^2 = 21$$

4) $2x^2 + 2y^2 - 8x + 4y = -2$

$$x^2 + y^2 - 4x + 2y = -1$$

$$x^2 - 4x + \underline{4} + y^2 + 2y + \underline{1} = -1 + \underline{4} + \underline{1}$$

$$(x-2)^2 + (y+1)^2 = 4$$

5) $\frac{7x^2}{7} + \frac{7y^2}{7} - \frac{28y}{7} + \frac{14}{7} = 0$

$$x^2 + y^2 - 4y + 2 = 0$$

$$x^2 + y^2 - 4y + \underline{4} = -2 + \underline{4}$$

$$x^2 + (y-2)^2 = 2$$

6) $\frac{3x^2}{3} + \frac{3y^2}{3} + \frac{18x}{3} + \frac{6y}{3} = 0$

$$x^2 + y^2 + 6x + 2y = 0$$

$$x^2 + 6x + \underline{9} + y^2 + 2y + \underline{1} = 0 + \underline{9} + \underline{1}$$

$$(x+3)^2 + (y+1)^2 = 10$$

Directions: Write the equation of the circle in GENERAL form.

7) $(x-2)^2 + (y+6)^2 = 25$

$$x^2 - 4x + 4 + y^2 + 12y + 36 = 25$$

$$\boxed{x^2 + y^2 - 4x + 12y + 15 = 0}$$

8) $(x+5)^2 + y^2 = 27$

$$x^2 + 10x + 25 + y^2 = 27$$

$$\boxed{x^2 + y^2 + 10x - 2 = 0}$$

Directions: Write the equation of the circle in both forms.

9) Center: (2, -3) & Radius: 7

Std: $(x-2)^2 + (y+3)^2 = 49$

General: $x^2 - 4x + 4 + y^2 + 6y + 9 = 49$

$$x^2 + y^2 + 4x + 6y - 36 = 0$$

10) Center: (-13, -16) & Point on the Circle: (-10, -16)

$d=r=3$

Std: $(x+13)^2 + (y+16)^2 = 9$

General: $x^2 + 26x + 169 + y^2 + 32y + 256 = 9$

$$x^2 + y^2 + 26x + 32y + 416 = 0$$

11) Ends of the diameter are (18, -13) and (4, -3)

midpt: (11, -8) $r = \sqrt{74}$

Std: $(x-11)^2 + (y+8)^2 = 74$

General: $x^2 - 22x + 121 + y^2 + 16y + 64 = 74$

$$x^2 + y^2 - 22x + 16y + 111 = 0$$

12) Center (0, 13) & Area of 25π $r=5$

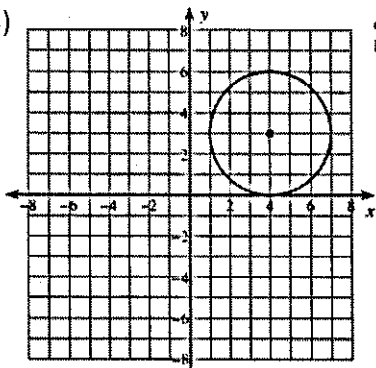
Std: $x^2 + (y-13)^2 = 25$

General: $x^2 + y^2 - 26y + 169 = 25$

$$x^2 + y^2 - 26y + 144 = 0$$

25

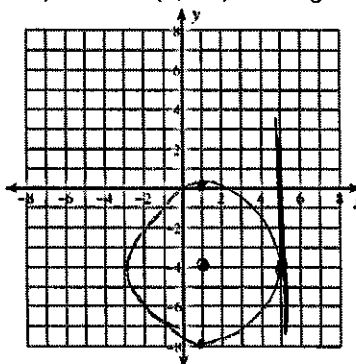
13)



Std: $(x-4)^2 + (y-3)^2 = 9$

General: $x^2 + y^2 - 8x - 6y + 16 = 0$

14) Center (1, -4) & Tangent to $x=5$



Std: $(x-1)^2 + (y+4)^2 = 16$

General: $x^2 + y^2 - 2x + 8y + 1 = 0$